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Optimization Of Fuzzy C-Means Clustering Algorithm With Combination Of Minkowski And Chebyshev Distance Using Principal Component Analysis

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Abstract Optimization is used to find the maximum or minimum of a function. In this research, optimization is applied to the objective function of the FCM algorithm. FCM is an effective algorithm for grouping data, but it is often trapped in local optimum solutions. Therefore, the similarity measure in the clustering process using FCM is very important. This study uses a new method, which combines the Minkowski distance with the Chebyshev distance which is used as a measure of similarity in the clustering process on FCM. The amount of data that is quite large and complex becomes one of the difficulties in providing analysis of multivariate data. To overcome this, one of the techniques used is dimensional reduction using Principal Component Analysis (PCA). PCA is an algorithm of the dimensional reduction method based on the main components obtained from linear combinations, which can help stabilize cluster analysis measurements. The method used in this research is dimensional reduction using PCA, clustering using FCM with a combination of Minkowski and Chebyshev distances (FCMMC), and clustering evaluation using the Davies Bouldin Index (DBI). The purpose of this research is to minimize the objective function of FCM using new distances, namely the combination of Minkowski and Chebyshev distances through the assistance of dimensional reduction by PCA. The results showed that the cluster accuracy of the combined application of the PCA and FCMMC algorithms was 1,6468. Besides, the minimum value of the combined objective function of the two methods is also obtained, namely 0,0373 which is located in the 15th iteration, where this value is the smallest value of the 100 maximum iterations set.

Keywords: PCA, Fuzzy C-Means, Minkowski and Chebyshev Distance, Davies Bouldin Index

1. Introduction

Optimization is everywhere, although it can mean different things from another perspective. From basic calculus, optimization can be easily used to find the maximum or minimum of a function [15]. Techniques in optimization with or without using gradient information, depending on

the suitability of the problems that arise [15]. Unconstrained optimization is a problem consideration in performing objective functions on real variables without constraints on values. The simple unconstraint optimization problem allows the maxima or minima of a univariate function $f(x)$ to be $-\infty < x < +\infty$ (or the

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entire real domain $\mathbb{R}$), it can be written (Yang, 2018) :
$$\max \ or \min f(x), x \in \mathbb{R}.$$

for an unconstrained optimization problem, optimally occurs at the critical point given the stationary condition $f'(x) = 0$. However, this stationary state is just a necessary condition, not a sufficient condition. If $f'(x_*) = 0$ and $f''(x_*) > 0$, this is the local minimum. Conversely, if $f'(x_*) = 0$ and $f''(x_*) < 0$, then this is the local maximum.

Whatever the problem in the real world, it is usually possible to formulate a constraint optimization problem in the general form [15]:
$$max/min_{x \in \mathbb{R}} f(x), x = (x_1, x_2, \dots, x_n)^T \in \mathbb{R}^n$$
subject to
$$h_i(x) = 0, (i = 1,2,3, \dots, M),$$
$$g_j(x) \leq 0, (j = 1, \dots, N),$$
where, $f(x), h_i(x)$, and $g_j(x)$ are scalar functions of the real vector x. There are M equality constraints and N inequality constraints. In general, all function problems $[f(x), h(x),$ and $g(x)]$ are nonlinear, requiring sophisticated optimization techniques.

Data with large dimensions, when the algorithm is applied to the grouping method, usually takes time to require. Therefore, the dimensional reduction can be used to overcome this. The dimension reduction method used in this study is Principal Component Analysis (PCA). PCA is an unsupervised multivariate analysis method that is effective for extracting high-dimensional data into low-dimensional space without data variables, using linear algebraic techniques to reduce dimensions that have interconnected variables into new data with unrelated ones called the main components [4]. Even though the data

dimensions are smaller, there won't be much information because the variance of data is maintained at least 70 - 80% [13].

Several studies related to the application of PCA to improve the performance of the clustering method have been carried out before, for example, a research conducted by [14]. The research resulted in high performance in determining the detail of fusion images. Another research was also conducted by [11], which was applied to the field of image processing and produced a level of 92,5%. The application of PCA which was then followed by the Fuzzy C-Means method was also carried out by previous researchers, namely [2]. This study discusses the algorithm for monitoring stations to monitor various sources of air pollution, as well as checking the zone in pollution. In this research, PCA is used as a method for monitoring the sources of air pollution, while the Fuzzy C-Means algorithm is used for the grouping stage of the monitoring stations. This study uses Euclidean distance as a measure of similarity and dissimilarity between objects in the dataset. There is also another research conducted by [16]. The research proposed an approach of mechanical failure information extraction and recognition in the early fault state variables, combined with the Principal Component Analysis (PCA) algorithm with FCM algorithm. The application results of this method to identify variables deviation fault rotor test bed are acceptable.

Research on the application of Principal Component Analysis (PCA) has been conducted by previous researchers, including research by [1]. This research resulted in a high accuracy rate of 96,07% by combining PCA and Levenberg-Marquardt Backpropagation (LMBP). Also, there is other research about PCA by [8]. This study aims to examine network

interference. The results obtained are as many as 10 main components with an accuracy rate of 99,7%. Another study was also conducted by [3]. This study uses PCA as a method in reducing the dimensions of features in animals so that the output of PCA will be used in the classification using the Logistic Regression (LR) method. The accuracy obtained from the research is 90%.

Fuzzy C-Means is a very effective algorithm, but the random values at the center point make iterative processes falling on the optimal local solution easy. The choice and size of inequality play an important role in the cluster structure of the data.

The use of the Fuzzy C-Means algorithm in the clustering process has been carried out by several researchers before, one of which is the research conducted by [6], who is engaged in the health sector to discuss the segmentation of brain tumors in patients using the Fuzzy C-Means and K-Way algorithms. The results obtained are that Fuzzy C-Means have better K-Means performance because the resulting segmentation is more precisely identified.

In this study, researchers used the new distance proposed by [12] by combining the Minkowski and Chebyshev distances. This distance has been applied to the classification using the K-Nearest Neighbors (KNN) method and produces a high degree of accuracy [12].

2. Preliminaries

2.1 Dimensional Reduction

Dimensional reduction is a method of reducing dimensions on a dataset by applying certain considerations [5], namely maintaining the information contained in the dataset even though the data is undergoing a reduction process, and producing a smaller number of variables that will simplify and speed up the process. computing and data visualization. Dimensional reduction can help stabilize the measurement for additional statistical analysis such as regression analysis or cluster analysis.

PCA is an unsupervised multivariate analysis method that is effective for extracting high-dimensional data into low-dimensional space without losing data characteristics, using linear algebraic techniques to reduce dimensions that have interrelated variables into new data with unrelated variables called principal components. [4]. Even though the data dimensions are smaller, it will not lose much information because data variance is maintained at least 70 - 80%. PCA is done to obtain the main components (principal components) that can explain most of the variance of data or can be said to be able to maintain most of the information measured using only a few variables which are the main components.

The calculation of PCA is based on the calculation of eigenvalues and eigenvectors which indicate the magnitude of the spread of data in a dataset. So, by using PCA, the initial variable is p variable will be reduced to k new variable which is called the principal component, with $k < p$. Even though it only uses k principal components, it is still able to produce the same value using the p variable [7]. The nature of the new variables formed from PCA is that the number of variables is less and has no correlation between the variables that are formed.

2.2 Clustering

Clustering is the process of grouping data based on the similarity between data in a

dataset, with learning without direction or so-called unsupervised. The clustered data will have the same level which is high in the same cluster but has a high degree of difference on different clusters. Grouping done on a data set is very important to obtain information, and make it easier to understand its elements. Clustering is divided into two methods, namely hard clustering and fuzzy clustering. In this hard clustering algorithm, several k-clusters will be formed, where each data will only be one cluster member. While in fuzzy clustering, each data is assumed to have the possibility to be a member of several clusters with different degrees for each group.

There are two basic methods in fuzzy clustering, the first is Fuzzy C-Means (FCM), so named because this clustering algorithm will be formed as many c-clusters that have been previously determined. Furthermore, the second method is Fuzzy Subtractive Clustering (FSC), wherein this method the number of clusters is not predetermined [9].

Fuzzy C-Means (FCM) was first introduced by Jim Bezdek in 1981 which is an algorithm of clustering using fuzzy grouping, so that data can be members of all classes or clusters with different degrees of 0 to 1. The concept of FCM, first determines the cluster location that will mark the average for each cluster, with the initial conditions being inaccurate. Each data point has a minimum degree for each cluster. In this condition, the cluster center and each data level return repeatedly, so it can be seen that the cluster center will move to the right location. This iteration is based on minimizing the objective function assigned to the cluster center weighted by the degree of each data.

2.3 Combined Distances Between Minkowski and Chebyshev

Rodrigues (2018) raises a new distance, namely the combination of Minkowski and Chebyshev distances. The combination of Minkowski and Chebyshev distances is shown in the equation below :

$$d_{(w_1,w_2,p)}(x,y) = w_1 \sqrt[p]{\sum_{k=1}^{n} |x_k - y_k|^p} + w_2 \, max_{k=1}^{n} |x_k - y_k| \tag{1}$$

where, x_k and y_k are the x and y values in the n dimension. When w_1 is greater than w_2 the distance is more like Minkowski. Conversely, if w_2 is greater than w_1 then the distance is more like Chebyshev.

2.4 Validity Index

Davies Bouldin Index (DBI) is one of the methods used to measure cluster validity in a clustering method. The purpose of measurement with DBI is to maximize the distance between clusters (inter-cluster) and to minimize the distance between data points (intra-cluster) in the same cluster. If the inter-cluster distance is maximum (large value), the similarity in characteristics between each cluster tends to be small, so that the differences between clusters are more pronounced. If the intra-cluster distance is minimum, then each data in the cluster has a high degree of characteristic similarity. A cluster will be considered to have an optimal clustering scheme if it has a minimal Davies Bouldin Index (DB) (close to 0) [10].

3. Result and Discussion

The FCMMC algorithm is applied to the result of dimensional reduction using PCA which has been calculated previously. Dimensional reduction using PCA was applied to hypertensive patient data with 5 original variables, resulting in 3 principal components (main components) as a linear combination between loading values and standardized data. Furthermore, the values of each data contained in the 3 main components are used as input in the clustering process using the Fuzzy C-Means method, a combination of the Minkowski and Chebyshev distance (FCMMC). Input data consisted of 100 patient data samples with 3 variables, namely PC_1, PC_2, and PC_3. The data will be grouped into 3 classes, namely class '1' for mild hypertension type, class '2' for moderate hypertension type, and class '3' for severe hypertension type. The following will display the data from the dimensional reduction by PCA.

Table 1. Data from PCA Dimension Reduction

No	PC_1	PC_2	PC_3
1	1,0952	1,3483	-0,1778
2	-1,3153	0,1893	1,7954
3	0,5015	-0,7913	-0,4487
⋮	⋮	⋮	⋮
99	-0,3543	0,9746	0,3117
100	-0,3945	-0,0928	-0,9341

The principle of the Fuzzy C-Means algorithm is minimize an objective function. The basic concept of Fuzzy C-Means, first determines the center of the cluster which will mark the average location for each cluster. At initial conditions, the center of this cluster is still inaccurate. Each data point has a degree for each cluster. By repeating the central cluster and the degree of each data point, it can be seen that the center of the cluster will move towards the right location. This iteration is based on minimizing the objective function which describes the distance from a given data point to the center of the cluster which is weighted by the degree of the data point [9]. The objective functions used in FCM with a combination of Minkowski and Chebyshev distances are:

$$min J_m(U,V) = \sum_{i=1}^{c} \sum_{k=1}^{n} (\mu_{ik})^m \left(w_1 \sqrt[l]{\sum_{j=1}^{p} |x_{kj} - v_{ij}|^p} \right.$$

$$\left. + w_2 max_{j=1}^{l} |x_{kj} - v_{ij}| \right)$$

subject to $\sum_{i=1}^{c} (\mu_{ik})^m = 1$

$0 < \mu_{ik} < 1$

where,

$J_m(U,V)$: objective functions with respect to U and V

c : number of clusters

n : the amount of data

m : weighter rank, $m \in [1,\infty)$

U : initial partition matrix

V : cluster center matrix

μ_{ik} : degree of kth data

$$SSW_i = \frac{1}{m_i} \sum_{j=1}^{m_i} d(x_j, c_i) \qquad (2)$$

$$SSB_{i,j} = d(c_i, c_j) \qquad (3)$$

$$R_{i,j} = \frac{SSW_i + SSW_j}{SSB_{i,j}} \qquad (4)$$

$$DBI = \frac{1}{k} \sum_{i=1}^{k} max_{i \neq j} (R_{i,j}) \qquad (5)$$

membership in the ith cluster

w_1 : Minkowski weights

w_2 : Chebyshev weights

x_{kj} : the kth data in the j variable
v_{ij} : the center of the ith cluster in the jth variable
p : Minkowski parameters.

The initial defined values for the grouping of data resulting from the reduction of dimensions, as follows $c = 3, w_1 = 3, w_2 = 2, p = 4, m = 2, maxiter = 100, \varepsilon = 10^{-5}$. Then, we obtain the initial partition random matrix that meets the constraints $\sum_{i=1}^{c}(\mu_{ik})^m = 1$. The partition matrix is shown as follows:

$$U^{(0)} = \begin{bmatrix} 0,1789 & 0,0786 & 0,7425 \\ 0,4496 & 0,3524 & 0,1980 \\ 0,1252 & 0,2773 & 0,5975 \\ \vdots & \vdots & \vdots \\ 0,2688 & 0,0819 & 0,6493 \\ 0,5351 & 0,4130 & 0,0520 \\ 0,7809 & 0,1588 & 0,0602 \end{bmatrix}.$$

Each data object has a certain degree of membership in each cluster. The value of the largest degree of membership shows the tendency of the data object to become a member of the cluster.

Furthermore, the cluster center is obtained for the first iteration, namely:

$$v_{ij}^{(1)} = \begin{bmatrix} -0,0550 & 0,0775 & 0,0152 \\ 0,0798 & -0,1368 & 0,0179 \\ 0,1184 & -0,0334 & -0,0164 \end{bmatrix}$$

where, $i = 1,2,3$ and $j = 1,2,3$.

The objective function that results from the first iteration is

$$F^{(1)} = \sum_{i=1}^{c}\sum_{k=1}^{n}(\mu_{ik})^m \left(w_1 \sqrt[p]{\sum_{j=1}^{l}|x_{kj} - v_{ij}|^p} \right.$$
$$\left. + w_2 max_{j=1}^{l}|x_{kj} - v_{ij}| \right) = 330,3307.$$

It is found that $\left| F_{FCMMC}^{(1)}(U,V) - F_{FCMMC}^{(0)}(U,V) \right| = 330,3307 > \varepsilon$, then proceed to iteration 2. Update the new partition matrix and calculate the center cluster in the second iteration using a sequential equation:

μ_{ik}

$$= \frac{\left(\dfrac{1}{\left(w_1 \sqrt[p]{\sum_{k=1}^{n}|x_{kj} - v_{ij}|^p} + w_2 max_{k=1}^{n}|x_{kj} - v_{ij}| \right)} \right)^{\frac{1}{m-1}}}{\sum_{k=1}^{n}\left(\dfrac{1}{\left(w_1 \sqrt[p]{\sum_{k=1}^{n}|x_{kj} - v_{ij}|^p} + w_2 max_{k=1}^{n}|x_{kj} - v_{ij}| \right)} \right)^{\frac{1}{m-1}}}$$

$$v_{ij} = \frac{\sum_{k=1}^{n}\mu_{ik}{}^m x_{kj}}{\sum_{k=1}^{n}\mu_{ik}{}^m}.$$

The iteration process will stop when it meets the stop condition, when $t > maxiter$ or when $\left| F_{FCMMC}^{(t)}(U,V) - F_{FCMMC}^{(t-1)}(U,V) \right| < \varepsilon$. The application of the FCMMC method which is carried out on the result of dimensional reduction with PCA, undergoes an iteration process stop when $t = 100$, this happens because it has met the stopping condition, namely $t > maxiter$.

The cluster center output in the last iteration when t = 100 was:

$v_{ij}^{(100)}$
$$= \begin{bmatrix} -0,0608 & 0,0816 & 0,0083 \\ 0,0222 & -0,0826 & 0,0078 \\ 0,0406 & -0,0022 & -0,0161 \end{bmatrix}, \begin{matrix} i & = & 1,2,3 \\ j & = & 1,2,3. \end{matrix}$$

The graph of the cluster center in the last iteration, when $t = 100$, is shown in the figure below.

Cluster Center

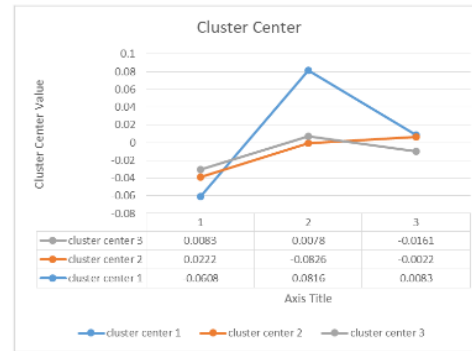| Axis Title	1	2	3
cluster center 3	0.0083	0.0078	-0.0161
cluster center 2	0.0222	-0.0826	-0.0022
cluster center 1	0.0608	0.0816	0.0083

cluster center 1   cluster center 2   cluster center 3

Figure 1. Centroid at t=100

Fuzzy C-Means has a weakness that is trapped in an optimum local solution. Of the 100 iterations carried out, the clustering process reached the minimum point at the time of the 15th iteration, with a value of 0,0373. The graph of the objective function values for each iteration is shown in the following figure:
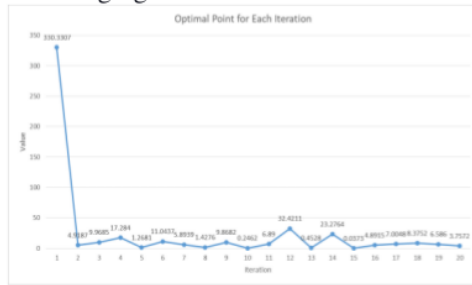

Figure 2. Value of the Objective Function of Each Iteration

As for the new partition matrix generated in the last iteration, when $t=100$ is

$$U^{(0)} = \begin{bmatrix} 0,3496 & 0,3142 & 0,3364 \\ 0,3386 & 0,3340 & 0,3273 \\ 0,2892 & 0,3760 & 0,3348 \\ \vdots & \vdots & \vdots \\ 0,3341 & 0,3208 & 0,3451 \\ 0,3715 & 0,2997 & 0,3289 \\ 0,3319 & 0,3288 & 0,3394 \end{bmatrix}.$$

So, from the new partition matrix generated in the last iteration when $t = 100$, the following clustering is obtained:

Table 2. FCMMC Clustering Results

Data	Group
1,2,4,6,7,8,9,10,11,14,19,22,25, 26,27,29,34,35,38,41,48, 49,51,54,57,58,59,63,66,67,68, 69,70,71,73,76,77,79,80, 81,82,83,84,87,93,94,95,96,97, 99	1
33,36,37,42,56,92	2
3,5,12,13,15,16,17,18,20,21,23, 24,30,31,32,39,40,43,44,	3

45,46,47,50,52,53,55,60,61,62, 64,65,72,74,75,78,85,86, 88,89,90,91,98,100

The results of clustering using the Fuzzy C-Means algorithm with a distance between Minkowski and Chebyshev (FCMMC), namely the data in group 1 is included in the mild hypertension class, data in group 2 is included in the moderate hypertension class, and data contained in group 3 is included in class severe hypertension.

Each data resulted from the FCMMC clustering process, each grouped according to the resulting cluster. The SSW values are obtained as follows:

$$\begin{aligned} SSW_1 &= 5,4171 \\ SSW_2 &= 3,9744 \\ SSW_3 &= 7,6456. \end{aligned}$$

Furthermore, the value of SSB obtained from the calculation results is

$$\begin{aligned} SSB_{12} &= 6,3353 \\ SSB_{13} &= 7,5549 \\ SSB_{23} &= 8,5845. \end{aligned}$$

Thus, the DBI value obtained is 1,6468. This DBI value is a measure of the accuracy of the clustering results.

4. Conclusion

In this paper, we introduce a new distance, namely the combination of Minkowski and Chebyshev distances as a similarity measure applied to the clustering process using Fuzzy C-Means. Besides, this paper also combines the PCA algorithm into Fuzzy C-Means with the Minkowski and Chebyshev Distance

Combination, as an effort to optimize the clustering process. The applications of these methods are new because previously there were no researchers who combined the two methods.

Based on the results and discussion of this study, it can be concluded that the PCA calculation produces 3 new variables as the main component (principal component) of the 5 variables studied, where the main component is the factor that most influences one's hypertension. Furthermore, the clustering accuracy obtained for the FCMMC which is applied to the dimensional reduction data with PCA has an accuracy value of 1.6468 and the minimum point of 100 iterations in the FCMMC process is achieved at the time of the 15th iteration which is 0.0373.

References

1. Adiwijaya, Untari N W, E Lisnawati, et al.: Dimensionality Reduction Using Principal Component Analysis For Cancer Detection Based on Microarray Data Classification. Journal of Computer Science (2018)
2. Dogruparmak S C, et al.: Using Principal Component Analysis and Fuzzy C-Means Clustering for The Assesment of Air Quality Monitoring. APR (2014)
3. Doraikannan S, Prabha S, Vijay K B.: Principal Component Analysis For Dimensionality Reduction For Animal Classification Based on LR. IJITEE (2019)
4. Farjo et al.: Does Principal Component Analysis Improve Cluster-Based Analysis?. IEEE (2013)
5. Han J, Kamber M.: Data Mining: Concepts and Techniques. Morgan Kaufmann (2006)
6. J Alan, S Ravi, M Sambath.: Brain Tumor Segmentation Using K-Means Clustering and Fuzzy C-Means Algorithms and Its Area Calculation. IJIRCCE (2014)
7. Johnson A R, Dean W W.: Applied Multivariate Statistical Analysis. Pearson Practice Hall (2007)
8. Keerthi Vasan K, B Surendiran.: Dimensionality Reduction Using Principal Component Analysis For Network Instrusion Detection. Elsevier GmbH (2016)
9. Kusumadewi S, H Purnomo.: Aplikasi Logika Fuzzy Untuk Pendukung Keputusan. Graha Ilmu (2010)
10. Mustofa Z, Imam S S.: Algoritma Clustering K-Medoids Pada E-Government Bidang Information and Communication Technology Dalam Penentuan Status Edgi. Jurnal Teknologi Informasi dan Komunikasi. (2018)
11. Panna M B.: Human Face Detection Based on Combination of Linear Regression, PCA and Fuzzy C-Means Clustering. IJCSIS (2019)
12. Rodrigues E O.: Combining Minkowski And Chebyshev: New Distances Proposal And Survey Of Distances Metrics Using K-Nearest Neighbours Classifier. Elsevier (2018)
13. Timm Neil H.: Applied Multivariate Analysis. Springer-Verlag (2002)
14. Vijarayan R, Muttan S.: Fuzzy C-Means Clustering Based Principal Component Averaging Fusion. International Journal of Fuzzy Systems (2014)

15. Yang Xin-She.: Optimization Techniques and Applications with Example. John Wiley&Sons (2018)

16. Zhao Qiang.: The Study on Rotating Machinery Early Fault Diagnosis based on Principal Component Analysis and Fuzzy C-Means Algorithm (2013)

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12 Brezis, H, K C Chang, S J Li, and P Rabinowitz. "Computational theory and methods for finding multiple critical points", Topological Methods Variational Methods and Their Applications, 2003.
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