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Fast Hard Clustering Based on Soft Set Multinomial Distribution Function

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Abstract. Categorical data clustering is still an issue due to difficulties/complexities of measuring the similarity of data. Several approaches have been introduced and recently the centroid-based approaches were introduced to reduce the complexities of the similarity of categorical data. However, those techniques still produce high computational times. In this paper, we proposed a clustering technique based on soft set theory for categorical data via multinomial distribution called Hard Clustering using Soft Set based on Multinomial Distribution Function (HCSS). The data is represented as a multi soft set where every soft set have its probability to be a member of the clusters. Firstly, the corrected proof is shown mathematically. Then, the experiment is conducted to evaluate the processing times, purity and rand index using benchmarks datasets. The experiment results show that the proposed approach have improve the processing times up to 95.03% by not compromising the purity and rand index as compared with baseline techniques.

Keywords: Clustering · Categorical data · Multi soft set · Multinomial distribution function

List of Symbols and Abbreviations

S: Information system/information Table

 $S_{\{0,1\}}$: System with value $\{0,1\}$

U: Universe

|U|: Cardinality of U U: Object of U

A: Set of Attribute/Variables

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a: Subset of attributeE: Parameter in soft set

i: Index i
 j: Index j
 k: Indek k
 l: Index l

e: Subset of parameterV: Domain Value set

 V_a : Domain (values set) of variable a

f: Information Function
F: Maps parameter function

y: Object

 $P(U_{\square})$ Power of Universe

 (F, \overline{A}) : Soft set

F(a): Soft set of parameter a

 $C_{(F,E)}$: Class soft set P: Probability

 p_i : Probability for each trial i $f(x, a_k)$: Probability mass function

 n_i, N_i : Number of Trial i

λ: Probability of multinomial distribution

 C_k : Cluster k

K: Number of clusters z_{ik} : Indicator function

 $CML(z, \lambda)$: Conditional maximum likelihood function $MaximizeL_{CML}(z, \lambda)$: Maximizing the log-likelihood function

 $L_{CML}(z, \lambda, w_1, w_2)$: Lagrange function

 w_1 : Lagrange multiplier constrains 1 w_2 : Lagrange multiplier constrains 2

HCSS: Hard Clustering using Soft Set based on Multinomial Distribu-

tion Function

1 Introduction

Clustering is the process of partitioning data sets from multiple variables into groups. The clustering problem often arises in the fields like image processing [1], pattern recognition [2], control system [3]. Until now, the most popular algorithm from various clustering algorithms that have been developed is k-means algorithm [4], 4, 5]. It produces efficiency and effectiveness in clustering with a large amount of data sets. However, k-means clustering algorithm unable to solve data sets that has categorical variables. The algorithm is only able to minimize a numerical cost function. Nevertheless, the k-means clustering algorithm was improved by Huang [4] into the k-modes clustering algorithm to eliminate the numeric-only limitation. Since then, the k-modes algorithms began to make major improvement such as the improvement of k-modes clustering using new dissimilarity

measures [6–8] and k-modes algorithm based on fuzzy set [9, 10]. Another algorithms least sum of square based for non-parametric approach clustering has been discussed in [11 60].

Due to its relative good performance, some improved versions of k-modes [15–17] have been proposed using more effective dissimilarity measurements to distinguize the importance of different attribute values. Furthermore, Kim et al. [18] proposed the use of fuzzy centroids approach to upgrade the efficiency of fuzzy k-modes. It has been improved by [19] to handle mix data numerical and categorical data based on genetic algorithm. Also, the fast clustering is still in concern currently especially in large dataset [3, 20, 21]. Another problem in tegorical data is there are no inherent distance measure object to another object. The clustering algorithms developed for managing numerical a cannot directly be used to cluster categorical data [11]. Thus, the challenging of categorical data clustering is more than the numerical. Since categorical data is regularly watched as tallies coming about from a settled number of trials in which each trial comprises of making one determination from a prespecified set of categories. The categorical data can be assumed as from trial independent following the multinomial distribution. Thus, the parametric approach is gore suitable for categorical data [22]. In [23] discussed some of parametric approach for categorical data clustering. However, almost all categorical data clustering techniques listed in [19] represent binary data sets. The problem with the aforementioned methods is that they have a long computation time and a low cluster purity.

On the other hand, categorica data have multi-valued attribute where it can be represented as a multi soft set [24]. The theory of soft set proposed by Molodtsov [25] is method for dealing with uncertainties in data. Some exiting clustering echniques based on soft set theory have been proposed in [26–27]. When compared to the theories of fuzzy set, probability, and interval mathematics, one of the key advantages of soft set theory is that it is free of the insufficiency of the parameterization tools. Whereas, the concept of multi-soft sets proposed by [24] is used for a multi-valued information systems to be applied to the categorical data without representing data in the binary values [24]. Thus, we would like to propose a Fast Hard Clustering based on Soft Set Multipornial Distribution Function to cluster the categorical data.

The rest of the paper is organized as follows Sect. 2 describes related works on information system, soft set, multinomial distribution. Section 3 constructs the mathematical modelling of the problem and proper the solution mathematically. Section 4 runs the computation experiment on data set. Finally, we conclude our work in Sect. 5.

2 Related Works

This section describes the basic of Information system, soft set theory and multinomial distribution.

2.1 Information System

Let's tuple S = (U, A, V, f), where U represents the univer 44 of objects, A be a set of variables or parameters, V is a domain (values set) of variable $a \subset A$ and the information

function is a total function as in Eq. (1) such that $f(u, a) \in V_a$, $\forall_{(u,a)\in U\times A}$.

$$f: \stackrel{\textbf{28}}{U} \times A \to V. \tag{1}$$

Definition 3 Given S = (U, A, V, f) as an information system. Suppose that $a \in A$, $V_a = \{0, 1\}$, then S is a bivalued information system, and can be defined as $S_{\{0,1\}}$.

$$S_{\{0,1\}} = \left(U, A, V_{\{0,1\}}, f\right). \tag{2}$$

Obviously, for every $u \in U$, $f(u, a) \in \{0, 1\}$, for every $a_i \in A$ and $v \in V$, the map a_i^v of U is $a_i^v : U \to \{0, 1\}$, such that

$$a_i^{\nu} = \begin{cases} 1 & f(u, a) = \nu \\ 0 & otherwise \end{cases}$$
 (3)

2.2 Soft Set Theory

Soft set [25, 26] a mathematical method for dealing with uncertainty via appropriate parametrization. Let U be an universe set, E be a set of parameters and $A \subset E$, F be the function that maps parameter A into the set of all subsets of the set U as shown in Eq. (4).

$$F: A \to P(U). \tag{4}$$

Then, the pair of (F, A) is called as soft set over U. $\forall_{a \in A}, F(a)$ be considered as the set of a-approximate elements of (F, A).

Consider to an information system definition, a soft set can be interpreted as a special type of information systems, termed a binary-valued information.

Proposition 1. Each Soft set (F, A) can be defined as $S_{\{0,1\}}$.

Proof: Lets the set of universe U in (F, E) can be considered as the universe U, the set of parameters denoted by E where $A \subset E$. Next, the function of the information system, f is written as:

$$f = \begin{cases} 1, \ u \in F(e) \\ 0, \ u \notin F(e) \end{cases} . \tag{5}$$

That is, when $u_i \in F(e_j)$, where $u_i \in U$ and $e_j \in E$, then $f(u_i, e_j) = 1$, otherwise $f(u_i, e_j) = 0$. To thus, we have $V(h_i, e_j) = \{0, 1\}$. Therefore, for $A \in E$, (F, A) can be represented as $(U, A, V_{\{0,1\}}, f)$. Thus, based on Definition 1, it can be defined as $S_{\{0,1\}}$.

Definition 2. The value-class of the soft set denoted by $C_{(F,E)}$ are the class of all value sets of a soft set (F,E).

Based on Proposition 1, A Boolean 23 lued information system deals with the "stan-3ard" soft set For a categorical value of information system denoted by S = (U, A, V, f) with $V = \bigcup_{a \in A} V_a$ and V_a states the domain of attribute a. The domain V_a has categorical values or multi values. A decomposition can be constructed from S into |A| number of Boolean-valued information system $S = (U, A, V_{\{0,1\}}, f)$. The decomposition of $A = \{a_1, a_2, \dots, a_{|A|}\}$ into the disjoint-singleton attribute $\{a_1\}, \{a_2\}, \dots, \{a_{|A|}\}$ is the basis of decomposition of S = (U, A, V, f).

Definition 3. [24] Suppose that S = (U, A, V, f) is a categorical-valued information 29 tem and a Boolean-valued information system is expressed by $S = (U, a_i, V_{a_i}, f)$, $i = 1, 2, \dots |A|$ with

$$S = (U, A, V, f) = \begin{cases} S^{1} = (U, a_{1}, V_{\{0,1\}}, f) \Leftrightarrow (F, a_{1}) \\ S^{2} = (U, a_{2}, V_{\{0,1\}}, f) \Leftrightarrow (F, a_{2}) \\ \vdots \\ S^{|A|} = (U, a_{|A|}, V_{\{0,1\}}, f) \Leftrightarrow (F, \overline{a}_{|A|}) \end{cases} = ((F, a_{1}), (F, a_{2}), \cdots, (F, a_{|A|})).$$
(6)

Furthermore, a multi soft set over universe U representing a capegorical-valued information system S = (U, A, V, f) is expressed as $(F, E) = ((F, a_1), (F, a_2), \cdots, (F, a_{|A|}))$.

2.3 Multinomial Distribution

A gradination of the binomial distribution is the multinomial distribution [29]. Lets N_i be the number of results in category i in a series of independent trials a with probability p_i for each trial, where, $1 \le i \le m$, $\sum_{i=1}^{m} p_i = 1$. Then for each m-tuple of non-negative integers (n_1, n_2, \ldots, n_m) with sum n.

$$P(N_1 = n_1, N_2 = n_2, \dots, N_m = n_m) = \frac{n!}{n_1! n_2! \dots n_m!} p_1^{n_1} p_2^{n_2} \dots p_m^{n_m}.$$
 (7)

Example 1. Suppose, there are 10 balls in a bas 20 consists 2 red balls, 3 green balls and 5 blue balls. From the basket, 4 balls will be selected, with replacement. Then, the probability of drawling 2 green balls and 2 blue balls is

$$P(n_1 = 0, n_2 = 2, n_3 = 2) = \frac{4!}{0!2!2!} 0.2^0 0.3^2 0.5^2 = 0.135.$$

A multinomial distribution with parameter $a_k = (a_k^{jl}, l = 1, ..., m_j, j = 1, ..., p)$ can be described as the probability mass function as follows;

$$f(x, a_k) = \prod_{i=1}^{p} \prod_{l=1}^{m_j} \left(a_k^{jl} \right)^{x^{jl}}, \tag{8}$$

where $\sum_{i=1}^{m_j} a_k^{jl} = 1$. The generic polytomous variable j(j = 1, ..., p) consist of categories m_j , and $m = \sum_{j=1}^p m_j$ indicates the total number of levels.

8

3 Hard Clustering Using Soft Set Based on Multinomial Distribution Function (HCSS)

Assume that U is a random sample size |U| from distribution $f(y, \lambda)$. A part on $U = \{u_1, u_2, \dots, \underbrace{15}_{15}\}$ into K cluster $C = \{c_1, c_2, \dots, c_K\}$ by indicator z_{ik} where $z_{ik} = 1$ if $u_i \in c_k$ and $z_{ik} = 0$ if otherwise. Then, the cluster joint distribution function on cluster C can be defined as $\prod_{k=1}^{K} \prod_{u \in C} z_{ik} f_{k}(y, \lambda)$.

on cluster C can be defined as $\prod_{k=1}^K \prod_{u_i \in c_k} z_{ik} f_k(y, \lambda)$.

To the pair (F, A), select it to multi-soft set over U which represents a categorical-valued information system S = (U, A, V, f), with $(F, a_1), \dots, (F, a_{|A|}) \subseteq (F, A)$ and $(F, a_{j1}), \dots, (F, a_{j|a_j|}) \subseteq (F, a_j)$. Suppose that λ_{kjl}^i is a probability of $u_i \in (F, a_{jl})$ into cluster $C_k, k = 1, 2, \dots, K, i = 1, 2, \dots, |U|, j = 1, 2, \dots, |A|$ and $l = 1, 2, \dots, |a_j|$, thus, the MMD of multi soft set can be written as

$$f_k(y, \lambda) = \prod_{j=1}^{|A|} \prod_{l=1}^{|a_j|} \left(\lambda_{kjl}^i\right)^{|F, a_{j_l}|}, where \sum_{l=1}^{|a_j|} \lambda_{kjl} = 1, \forall k, j.$$
 (9)

Thus, the objective function of the clustering is to find the highest probability (λ) of the conditional maximum likelihood function as in (10) to assign the U to cluster C.

$$CML(z,\lambda) = \prod_{k=1}^{35} \prod_{i=1}^{|U|} z_{ik} \prod_{j=1}^{|A|} \prod_{l=1}^{|a_j|} \left(\lambda_{kjl}^i\right)^{|F,a_{j_l}|}.$$
 (10)

where

$$\sum_{k=1}^{K} z_{ik} = 1, z_{ik} \in \{0, 1\} \text{ for } i = 1, 2, \dots, |U|.$$

$$\sum_{l=1}^{|a_j|} \lambda_{kjl} = 1.$$

Equation (10) is equivalent to maximizing the log-likelihood as in (11).

$$MaximizeL_{CML}(z, \lambda) = \sum_{k=1}^{K} \sum_{i=1}^{|U|} z_{ik} \prod_{j=1}^{|A|} \prod_{l=1}^{|a_{j}|} \left(\lambda_{kjl}^{i}\right)^{|F, a_{j_{l}}|}$$

$$= \sum_{k=1}^{K} \sum_{i=1}^{|U|} z_{ik} \sum_{j=1}^{|A|} \sum_{l=1}^{|a_{j}|} \ln \left(\lambda_{kjl}^{i}\right)^{|F, a_{j_{l}}|}.$$
(11)

Subject to

$$\sum_{k=1}^{K} z_{ik} = 1, z_{ik} \in \{0, 1\} \text{ for } i = 1, 2, \dots, |U|.$$

$$\sum_{l=1}^{|a_j|} \lambda_{kjl} = \mathbf{1}.$$

Proposition: Lets (F, a_j) be a soft 32 over U which represents a categorical-valued information 6 stem with $(F, a_1), \dots, (F, a_{|A|}) \subseteq (F, A)$ and $(F, a_{j_1}), \dots, (F, a_{j|a_j|}) \subseteq (F, a_j)$. Suppose $(F, a_1), \dots, (F, a_{|A|}) \subseteq (F, A)$ and $(F, a_{j_1}), \dots, (F, a_{j|a_j|}) \subseteq (F, a_j)$ be a multi soft set of U. Then z_{ik} and λ_{kjl} are local maximum for $L_{CML}(z, \lambda)$ if only if

$$\lambda_{kjl} = \frac{\sum_{u_i \in (F, a_{j_l})} z_{ik}}{\sum_{l=1}^{|a_j|} \sum_{u_i \in (F, a_{i_l})} z_{ik}},\tag{12}$$

$$z_{ik} = \begin{cases} 1 & if \sum_{j=1}^{|A|} \ln(\lambda_{kjl}^i) = \max_{1 \le k' \le K} \sum_{j=1}^{|A|} \ln(\lambda_{kjl}^i) \\ 0 & otherwise \end{cases}$$
 (13)

Proof. The maximizing problem in Eq. (11) is equivalent to the Lagrangian function of L_{CML} as in (14).

$$L_{CML}(z, \lambda, w_1, w_2) = \sum_{i=1}^{36} \sum_{k=1}^{K} \sum_{j=1}^{K} \sum_{l=1}^{|\vec{a}_j|} \ln \left(\lambda_{kjl}^i \right)^{|F, a_{j_l}|} - w_1 \left(\sum_{k=1}^{K} z_{ik} - 1 \right) - w_2 \left(\sum_{l=1}^{|a_j|} \lambda_{kjl} - 1 \right)$$
(14)

By take the first derivative of the Lagrangian L_{CML} with respect to the z_{ik} , λ_{kjl} , w_1 , w_2 and set to be 0. The equation system obtained can be defined as follows

$$\frac{\partial L_{CML}}{\partial z_{ik}} = \sum_{i=1}^{|A|} \sum_{l=1}^{|a_i|} \ln \left(\lambda_{kjl}^i \right)^{|F, a_{j_l}|} - w_1 = 0, \tag{15}$$

$$\frac{\partial L_{CML}}{\partial \lambda_{kjl}} = \frac{\sum_{i=1}^{|U|} z_{ik} |F, a_{j_l}|}{\lambda_{kjl}} - w_2 = 0, \tag{16}$$

$$\frac{\partial L_{CML}}{\partial w_1} = -\left(\sum_{k=1}^K z_{ik} - 1\right) = 0,\tag{17}$$

$$\frac{\partial L_{CML}}{\partial w_2} = -\left(\sum_{l=1}^{|a_j|} \lambda_{kjl} - 1\right) = 0. \tag{18}$$

From (16)

$$w_2 = \frac{\sum_{i=1}^{|U|} z_{ik} |F, a_{j_l}|}{\lambda_{kil}}$$
 (19)

$$\lambda_{kjl} = \frac{\sum_{i=1}^{|U|} z_{ik} \left| F, a_{j_l} \right|}{w_2}$$

Substitute to (18)

$$\sum_{l=1}^{|a_{j}|} \lambda_{kjl} = \sum_{l=1}^{|a_{j}|} \frac{\sum_{i=1}^{|U|} z_{ik} |F, a_{j_{l}}|}{w_{2}}$$

$$1 = \frac{\sum_{l=1}^{|a_{j}|} \sum_{i=1}^{|U|} z_{ik} |F, a_{j_{l}}|}{w_{2}}$$

$$w_{2} = \sum_{l=1}^{|a_{j}|} \sum_{i=1}^{|U|} z_{ik} |F, a_{j_{l}}|$$
(20)

Substitute to (16), then

$$\sum_{l=1}^{|a_{j}|} \sum_{i=1}^{|U|} z_{ik} |F, a_{j_{l}}| = \frac{\sum_{i=1}^{|U|} z_{ik} |F, a_{j_{l}}|}{\lambda_{kjl}};$$

$$\lambda_{kjl} = \frac{\sum_{i=1}^{|U|} z_{ik} |F, a_{j_{l}}|}{\sum_{l=1}^{|a_{j}|} \sum_{i=1}^{|U|} z_{ik} |F, a_{j_{l}}|}$$
(21)

Then, for a given z, all the inner sums of quantity $\sum_{i=1}^{|U|} \sum_{k=1}^K z_{ik} \sum_{j=1}^{|A|} \sum_{l=1}^{|a_j|} \ln \left(\lambda_{kjl}\right)^{|F,a_{j_l}|}$ are non negative and independent. Maximizing the quantity is equivalent to maximizing the each inner sum. For 1 < k < K the inner sum the quantity as

$$\sum_{i=1}^{|U|} z_{ik} \sum_{j=1}^{|A|} \sum_{l=1}^{|a_{j}|} \ln\left(\lambda_{kjl}\right)^{|F, a_{j_{l}}|}$$

$$\Leftrightarrow \sum_{i=1}^{|U|} z_{ik} \left(\sum_{j=1}^{|A|} \sum_{l=1}^{|a_{j}|} \ln\left(\lambda_{kjl}\right)^{|F, a_{j_{l}}|}\right)$$

$$(22)$$

for 1 < i < |U|, z_{ik} is fix and non negative and for each $i = 1, 2, \ldots, |U|, |F, a_{j_l}| = 1$ if $u_1 \in (F, a_{j_l})$ and $|F, a_{j_l}| = 0$ if $u_1 \notin (F, a_{j_l})$, it follows that $\sum_{i=1}^{|U|} z_{ik} |F, a_{j_l}| = \sum_{u_i \in (F, a_{j_l})} z_{ik}, \forall_{u_i} \in U, i = 1, 2, \ldots, |U|$. Thus,

$$\lambda_{kjl} = \frac{\sum_{u_i \in (F, a_{j_l})} z_{ik}}{\sum_{l=1}^{|a_j|} \sum_{u_i \in (F, a_{j_l})} z_{ik}}$$
(23)

and inner sum $\sum_{i=1}^{|U|} \sum_{k=1}^{K} z_{ik} \sum_{j=1}^{|a_j|} \sum_{l=1}^{|a_j|} \ln\left(\lambda_{kjl}\right)^{|F,a_{j_l}|}$ maximize iff each term $\sum_{j=1}^{|A|} \sum_{l=1}^{|a_j|} \ln\left(\lambda_{kjl}\right)^{|F,a_{j_l}|} = \sum_{j=1}^{|A|} \ln\left(\lambda_{kjl}^i\right), \forall_{u_i} \in U, i = 1, 2, \dots, |U|, l = 1, 2, \dots, |a_j|$ is maximize. Thus,

$$z_{ik} = \begin{cases} 1 & if \sum_{j=1}^{|A|} \ln(\lambda_{kjl}^i) = \max_{1 \le k' \le K} \sum_{j=1}^{|A|} \ln(\lambda_{kjl}^i) \\ 0 & otherwise \end{cases}$$
 (24)

4 Computational Run on UCI Datasets

the experiment, MATLAB version 9.0.0.341360 (R2016a) is used to determine the rformance in terms of cluster purity, rand index and computational time of the HCSS and other two fuzzy k-based approaches. They executed sequentially on the specifications of a computer with an Intel Core i5, the total main memory is 8GB, agl the operating system is Mac OS High Sierra. The Experiment will be conducted on four categorical datasets obtained from the UCI Machine Learning Repository [30], namely Zoo, Spect, Monk and Car. The all techniques are run by 100 differences initial membership function randomly for each datasets. The average in term of cluster purity, Rank Index and Computational Time is captured in Fig. 1. It shows that the HCSS technique is able to maintain the cluster purity and Rank index compared by the FC and FkP. Nevertheless, The result of computation time indicates that HCSS overcome FC and FkP technique. In detail, FC and FkP respectively consume approximately 0.7017 s and 0.4615 s of execution time to Process four dataset in average. In contrast, PSS technique requires only approximately 0.031 s of execution time in average for four dataset. It clearly shows a improvement of execution time by 95.03% as in Table 1. Thus. the HCSS is superior in terms of computational time with able to maintenance the rank index and purity comparing to the baselines.

Zoo Monk Spect Car Average FC 0.8732 0.9206 0.7037 0.7037 0.7017 FkP 0.2617 0.3754 0.4645 0.0099 0.4615 HCSS 0.0236 0.0253 0.0995 0.0107 0.0310 Improvement 95.03%

Table 1. Comparison results in term of time responses

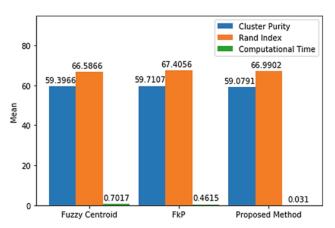


Fig. 1. Mean results of cluster purity, rand index, and computational time

5 Conclusion

The problem of fuzzy-based categorical data clustering can be overcome by several algorithms. However, these algorithms do not provide higher clusters purity and lower response times. Thus, the hard categorical data clustering based on soft set via multinomial distribution is proposed. The data is decomposed based soft set to become a multi soft set and multivariate multinomial distribution is used for clustering the data. Comparative analysis of the proposed algorithm called HCSS and two based and two based and the proposed approach out performs the existing approaches in technique. The results show that the proposed approach out performs the existing approaches in technique. In the future work, we will extend the proposed approach based on fuzzy to increase the performance of the technique.

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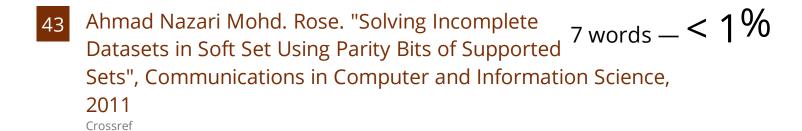
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