MOTION TRAJECTORY GENERATION BASED ON POLYNOMIAL METHOD FOR HUMANOID ROBOT

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Humanoid Robot is a robot whose shape and appearance resembles the human body and is equipped with technology so that it can carry out basic functions like humans in general. Robot Soccer Universitas Ahmad Dahlan (R-SCUAD) is one of Robotic Teams that competes on Indonesian Humanoid Robotic Soccer Competition. The focus of the competition is on developing humanoid robots that can play soccer, and each robot is equipped with sensors, actuators, and other supporting technologies to recognize the playing field, identify the ball, perform basic movements such as walking, kicking, standing up, communicating with teammates, and making decisions during the game.

One of the challenges in robot development is generating smooth and continuous movements. The currently used method of manual movement generation by the robot operator is often unsuccessful due to a lack of precision and consistency. Robots often fail to generate movements because the movements that have been recorded are not played coherently.

To address this issue, this research propose a trajectory generation method based on fourth-degree polynomial functions that allows for more precise control over the movement path. The operator can simply provide the robot with a target position and orientation, and the trajectory generates the necessary movement to reach the target. The main focus is on the robot's ability to generate kicking movements using this trajectory generation method. Results show that the robot successfully generated left, right, and side kicks, with an average time of 5.334 seconds for left kicks, 6.099 seconds for right kicks, and 3.88 seconds for side kicks, based on ten trials.

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1. INTRODUCTION

Humanoid Robot is a robot whose shape and appearance resembles the human body and is equipped with technology so that it can carry out basic functions like humans in general[1]. In a soccer game between humanoid robots, the robot is required to be able to walk dynamically, run and kick the ball while maintaining balance, visual perception of the ball and the pattern of the field, self-localization and teammates and recognizing opponents[2][3]. RoboCup is a humanoid robot football competition in the world, while in Indonesia itself, there is the KRSBI-Humanoid (Kontes Robot Sepakbola Indonesia - Humanoid).

Robot Soccer Universitas Ahmad Dahlan (R-SCUAD) is a robot team from Ahmad Dahlan University that conducts research and development in the field of humanoid soccer robots. Currently, R-SCUAD has five robots with capabilities such as ball detection and recognition, field image recognition, dynamic walking, ball kicking, ball chasing, getting up from a fall, and other abilities. The technology used by R-SCUAD undergoes continuous development every year to optimize the robots' potential and prepare them for participation in the Indonesia Robot Contest. The robot's movements are created using RoboPlus software. RoboPlus is a software developed by ROBOTIS that facilitates interaction with all ROBOTIS hardware devices, including control, dynamixel, sensors, and other components.

The current R-SCUAD robots have implemented several methods for generating movements. These include parametric walking motion generation using inverse kinematics and sinusoidal methods, as well as manual generation of basic motions using the record and play method. In the inverse kinematics method, motion generation is performed by analyzing the angle coordinates of the servos used within the robot's range of motion [4][5][6]. This method involves trial and error to achieve precise movement goals. The drawback of this method is the time-consuming process and significant memory usage[7].

On the other hand, in the record and play method, motion generation is based on the existing servos $[8][9]$. Each servo has its initialization with a unique ID number. Since the framework used is from Robotis, the robot comes equipped with basic motions like "Hi," "Bye," and "Talk". In the Indonesia Robot Contest, several specific motions are required for the robot. Meanwhile, other motions such as getting up when the robot falls, body rotation, arm extension for the goal keeper robot, and body dropping and kicking motions are still created using the record and play method. This involves recording the angle values of the servo's tilt and then calling the motion using motion commands in the main program $[10]$. The drawback of this method is that it takes a relatively long time, which can cause the servos to overheat and affect their performance[11].

Generating humanoid robot motion trajectories based on polynomials can be a solution to overcome constraints related to short and asymmetric movements[12]. Issues such as time-consuming motion calling often occur in short-distance movements[13][14]. This algorithm is proposed to generate smoother motion on trajectories defined by polynomial functions by combining two arbitrary conditions determined by the position of each joint $[15][16]$.

2. METHODS

The research was conducted using a humanoid robot, R-SCUAD, which moves using 12 MX-64 servo motors and 8 MX-28AR servo motors. The robot moves with OpenCM9.04 as the sub-controller, Odroid XU-4 as the central controller, and Gyroscope and Accelerometer as the robot's balance sensors. The robot's design is shown in **Fig 1.** The robot's framework is made of stainless steel with a thickness of 2.5mm for the robot's body, carbon fiber material with a thickness of 1.5mm for the robot's foot sole and 1mm for the robot's hand, acrylic with a thickness of 5mm for the robot's head support, and nylon with a thickness of 2mm as the robot's body protector.

Fig 1. The Robot

The size of the robot's framework greatly affects every movement it performs. The dimensions of the robot are presented in **Table 1.**

Dimension	Unit (cm)						
Height	62						
Hleg	28,5						
Hhead	14,5						
The width of the robot when the arms are stretched	69						
The width of the foot sole	8						
The length of the foot sole	12						
The length of the thigh links	11,5						
The length of the knee links	12.5						
The length of the foot sole link	4,2						

Table 1. Robot Dimension

The robot is actuated by 20 servo motors distributed throughout its body. Each servo is assigned a unique ID number during initialization, ensuring accurate data transmission and information retrieval between the servos during motion control. The detailed servo numbering is presented in **Table 2.**

2.1. The Robot Control sistem

Fig 2 shown the system of the utilized robot, wherein the servo angle coordinates are captured through Gyroscope and Accelerometer sensors located on the sub-controller board. The data is subsequently processed on the ODROID XU-4 as the central controller. The processed data is then transmitted to the OpenCM9.04 as the sub-controller, which further drives the actuators.

Fig 2. Block Diagram

Every planned process in the research can be observed through the flowchart in **Fig 3.** Once the robot reaches the desired position (close to the ball), the robot operator will initiate the selection of a specific action. Button 1 is used for a left kick, button 2 for a right kick, and button 3 for a side kick. Subsequently, the robot will stop after completing its task.

Fig 3. Flowchart

2.2. End effector and Trajectory Generation

 In order to develop movement patterns for the robot, it is essential to conduct an analysis of its legs to determine the range of motion and rotation that can be achieved. This analysis is crucial to ensure that the robot's movements are within the desired limits and are stable and precise[17][18]. **Fig 4.** shown diagram of the robot's leg is provided, with a yellow straight line representing the x-axis and a red line representing the zaxis[19]. The direction of rotation for the robot's leg is established as the z-axis. The robot's leg is designed with six degrees of freedom, which are allocated to each joint, including hip pitch, hip yaw, hip roll, knee pitch, ankle pitch, and ankle roll $[20][21]$. This journal emphasizes the importance of analyzing the robot's legs and joints in the development of movement patterns and ensuring the robot's stability and accuracy in its movements.

Fig 4. Rotation point on Robot Leg

Thus, **Table 3**. shown the coordinates of each frame that is connected to the servo dynamixel and the joints contained in the robot, each representing the angle of rotation (θ) and the range of motion that can be performed[19]. The Denavit-Hartenberg (D-H) table is a method used in robotics to model and describe the relationships between various joints in a robot. This table utilizes four parameters known as the Denavit-Hartenberg parameters. These parameters are as follows:

α : Twist angle

The twist angle represents the angle between the z_i -1 axis and the z_i -i axis, measured along the x_i axis. Geometrically, it is the rotation angle between the i-1th revolute axis and the ith revolute axis around the x_i axis.

a : Link length

The link length refers to the distance between the z_i-1 axis and the z_i axis, measured along the x_i axis. Geometrically, it is the distance between the i-1th revolute axis and the ith revolute axis, which are mutually perpendicular.

- **d** : Link offset The link offset represents the distance between the x_i -1 axis and the x_i axis, measured along the z_i-1 axis. Geometrically, it is the distance between the i-1th revolute axis and the ith revolute axis, which are parallel to each other
- **θ** : Sudut *joint* The joint angle describes the rotation between the x_i-1 axis and the x_i axis, measured along the z_i-1 axis. Geometrically, it is the rotation angle between the i-1th revolute axis and the ith revolute axis around the z_i-1 axis

In this process, the desired movement trajectory is created based on a polynomial function to generate movement from the initial position to the final position (destination point) [22]. Before carrying out the movement, the set point value, the intermediate angle position, and the continuation position and angle in generating a movement must be calculated in advance so that the resulting movement can be smoother[23][24]. The trajectory is designed using the 4 degree polynomial method where the 4th degree polynomial function represents the process initial to lift-off, set-down to the final position.

$$
p = a_1t^4 + a_2t^3 + a_3t^2 + a_4t + p_0
$$
 (1)

In this process, the problem of saving the robot's last movement when kicking must be solved. The tilt angle of the robot's body and legs will be used as a parameter so that the robot can generate movements according to the angle accurately and in a balanced position[19][25]. This problem can be solved using the rules of the 4x4 transformation matrix with the equation is as follow :

$$
T = \begin{pmatrix} \cos \theta & -\sin \theta^* \cos \alpha & \sin \theta^* \sin \alpha & a \cdot \cos \theta \\ \sin \theta & \cos \theta \cdot \cos \alpha & -\cos \theta \cdot \sin \alpha & a \cdot \sin \theta \\ 0 & \sin \alpha & \cos \alpha & d \\ 0 & 0 & 0 & 1 \end{pmatrix} \tag{2}
$$

The matrix is presented in 4x4 form as a representation of the position of the joints, and the orientation of the end-effector on the robot's legs mathematically. This matrix consists of a 3x3 rotation matrix, namely the orientation of the end-effector in space, and a 3x1 translation vector, namely the position of the end-effector relative to the reference. The last row [0 0 0 1] is used to maintain the homogeneity of the matrix.

2.3. MotionTime Step

 The speed of motion invocation is measured based on the angular values generated divided by the time taken by each joint to reach each position, from the initial pose to the final position. The position values are then converted and expressed in degrees (°) using Equation (3).

$$
x = value in position (360/Vmax)
$$
 (3)

Where:

 $X = angle$ value of the servo in degrees

 V max = maximum position value (4096)

2.4. Motion Time Step comparison

 The dynamic factor in this study is measured by dividing the speed of motion invocation by a unit of time. The result is then compared with the previous method, which is the record and play method. The speed of motion invocation from the record and play method is compared with the polynomial-based trajectory method using Equation (4), which calculates the average.

Average $=$ (Sum of Invocation Time) / (Number of data) (4)

3. RESULTS AND DISCUSSION

The testing was conducted in the Robotics Laboratory of the Electrical Engineering Department, 1st Floor, Campus 4, Ahmad Dahlan University, Yogyakarta. The robot was placed on a synthetic grass carpet, and the motion execution was performed by invoking pre-programmed movements through a dedicated software, developed specifically for the purpose of the experiment.

3.1 End Effector and Motion trajectory

Table 2. shown the Denavit Hartenberg on robot right leg.

From **Table 2**, it can be observed that several variables have a value of 0. Note that for the "a" variable on Hip yaw and Hip Roll are two opposing joints but have different joint configurations, as illustrated in **Fig 5.**

Fig 5. Joints, Links,and Rotation

The yellow circles in **Fig 5.** represent the joints on the robot leg, with corresponding numerical labels indicating the ID of the Dynamixel servo used. Theta (θ) denotes the angle at the joint around the rotational axis (z). Hip Yaw (servo ID 7) moves left and right within the horizontal plane with a range of +90 degrees (relative to Z0), while Hip Roll (servo ID 9) tilts sideways within the vertical plane by -90 degrees. The parameter α takes a value of 0 when the rotational axes of links i and i+1 do not intersect or align. There are three main links in the robot leg: from hip to knee, knee to ankle, and ankle to foot (with the foot base shaped like a square). The variable a represents the link length. Hip Pitch (servo ID 11) and Knee Pitch (servo ID 13) are connected by L1, Knee Pitch (servo ID 13) and Ankle Pitch (servo ID 15) are connected by L2, and Ankle Roll (servo ID 17) is connected to Ankle Pitch (servo ID 15) with the help of an H-shaped stainless structure at the front, which then extends directly to the foot using L3. The variable d is 0 because the rotational axis (z) intersects with the translational axis. The following is the process of determining the homogeneous transformation matrix of each joint using the formula in equation (2) :

$$
T1 = \begin{pmatrix} \cos \theta_1 + 90 & (-\sin \theta_1 + 90) & 0 & (90)(\cos \theta_1 + 90) \\ \sin \theta_1 + 90 & -(\cos \theta_1 + 90) & 0 & (90)(\sin \theta_1 + 90) \\ 0 & 0 & 1 & d1 \\ 0 & 0 & 0 & 1 \end{pmatrix}
$$

$$
T2 = \begin{pmatrix} \cos \theta_2 - 90 & (-\sin \theta_2 - 90) & 0 & (-90)(\cos \theta_2 - 90) \\ \sin \theta_2 - 90 & -(\cos \theta_2 - 90) & 0 & (-90)(\sin \theta_2 - 90) \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}
$$

$$
T3 = \begin{pmatrix} \cos \theta_3 & -\sin \theta_3 \cdot \cos \alpha_3 & \sin \theta_3 \cdot \sin \alpha_3 & 0 \\ \sin \theta_3 & \cos \theta_3 \cdot \cos \alpha_3 & -\cos \theta_3 \cdot \sin \alpha_3 & 0 \\ 0 & \sin \alpha_3 & \cos \alpha_3 & 0 \\ 0 & \sin \alpha_3 & \cos \alpha_3 & 0 \end{pmatrix}
$$

\n
$$
T4 = \begin{pmatrix} \cos \theta_4 & -\sin \theta_4 & 0 & 0 \\ \sin \theta_4 & \cos \theta_4 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}
$$

\n
$$
T5 = \begin{pmatrix} \cos \theta_5 & -\sin \theta_5 & 0 & 90 \cdot \cos \theta_5 \\ \sin \theta_5 & \cos \theta_5 & 0 & 90 \cdot \sin \theta_5 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}
$$

\n
$$
\cos \theta_6 & -\sin \theta_6 \cdot \cos \alpha_6 & \sin \theta_6 \cdot \sin \alpha_6 & 0 \cdot \cos \theta_6
$$

\n
$$
T6 = \begin{pmatrix} 0 & \sin \theta_5 & \cos \theta_6 & -\cos \theta_6 \cdot \sin \alpha_6 & 0 \cdot \sin \theta_6 \\ 0 & \sin \theta_5 & \cos \theta_6 & -\cos \theta_6 \cdot \sin \alpha_6 & 0 \cdot \sin \theta_6 \\ 0 & 0 & 0 & 0 \end{pmatrix}
$$

(0 0 0 1) The motion is generated using a fourth-degree polynomial-based trajectory method. **Tables 4.** and **5** below show the positions of each joint during the left kick motion, expressed in degrees (0) . The advantage of using a fourth-degree polynomial to generate the motion is the ability to smooth between key points and its computational efficiency. However, it may not be suitable for all types of trajectories, especially those with complex geometries or multiple obstacles. In this case, other mathematical functions or motion planning algorithms can be used.

```
double a1 = \frac{10}{24};
    double a2 = a0/6 - j0*pow(tf,2)/120 - jf*pow(tf,2)/24 - af*t/12 + j0*t/6 + j0*cf/6jf*tf/4;
    double a3 = 0.5*j0*pow(tf,3)/6 + jf*pow(tf,3)/6 + 0.5*a0*pow(tf,2) -
0.5*af*pow(tf,2) + j0*pow(tf,2)/2 + jf*pow(tf,2)/2 + v0*tf - vf*tf/2 - a0*tf/6 +
aff*tf/6;
   double a4 = -j0*pow(tf,4)/24 - jf*pow(tf,4)/24 - a0*pow(tf,3)/6 +af*pow(tf,3)/6 - j0*pow(tf,3)/6 - jf*pow(tf,3)/4 - v0*pow(tf,2)/2 +vf*pow(tf,2)/4 + a0*t/6 - af*t/12 - p0 + pf;
```
The scipt above defines a function that takes the initial and final states of a single degree of freedom, including position, velocity, acceleration, and jerk at time zero and the final position, velocity, acceleration, and jerk at the end of the trajectory, as well as the total trajectory time. The formula in equation (3.2) is used to create the trajectory pattern and is added to Listing 4.1 as follows:

```
for (double t = 0; t \leq tf; t += 0.01)
{
    double p = a1*pow(t,4) + a2*pow(t,3) + a3*pow(t,2) + a4*t + p0;traj.push back(p); }
```
The coefficients a1, a2, a3, and a4 are calculated based on the initial and final states as well as the total trajectory time. These coefficients are used to generate trajectory points for the degree of freedom over time using a loop that iterates from zero to the total trajectory time (tf) with an increment of 0.01 seconds. The trajectory points are stored in a vector called traj, which is returned at the end of the function. **Table 4.** shows the joint positions (in degrees/0) in the fourth-degree polynomial.

Fig 6. Polynomial Left Kick Graph

The initial value of the position can be calculated using Equation (3) to convert the servo position value (pose in) from the RoboPlus Motion software, which is presented as a value ranging from 0 to 4096, to degrees. For example, if the position value is 2048, the calculation for the angle value is as follows: $x = 2048 (360 / 4096)$

$$
x = 2048 (300)
$$

$$
x = 180
$$

Therefore, the servo position value of 2048, when expressed in degrees, is 180 degrees.

Table 5. Pose In Value with Record and Play

The motion is manually created by adjusting the initial position of the robot to the position when the robot is in the walk-ready position. **Figures 7. to 11** below depict the trajectory patterns from the record and play method, with each figure representing one joint, as each joint has a different pattern.

Fig 7. Left Kick – Hip Yaw

Fig 8. Left Kick – Hip Roll

Fig 9. Left Kick – Hip Pitch

Fig 11. Left Kick – Ankle Yaw

Fig 12. Left Kick – Ankle Roll

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Fig 14. Left Kick – Side View

Fig 15. Walk Ready

Fig 16. Lifting Left Leg

Fig 17. Swinging Left Leg

Fig 18. Kick The Ball

Fig 19. Swinging Left Leg

Table 6. Right Kick Position (degree) with Fourth Degree Polynomial **Joints Initial Value (o) Lift Off (o) Interval Final Value (o)** hip yaw R 180 175.176 200 198.090 L 180 180.000 200 180.000 hip roll R 180 190.452 200 184.724 L 165 173.266 200 180.905 knee R 125 243.518 200 131.156 L 230 211.106 200 228.392 ankle pitch R 230 300.180 200 229.482 L 125 129.316 200 136.528 Ankle yaw R 200 262.337 200 192.621 L 160 151.753 200 162.170 Ankle roll R 180 201.436 200 183.806 L 180 197.429 200 177.396

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Joints		position $(°)$						
		step 0	step 1	step 2	step 3	step 4	step 5	
	\mathbf{I} .	125.684	129.727	243.105	122.871	123.750	129.111	
ankle pitch	R	234.932	232.910	228.252	222.012	238.184	232.910	
		225.967	234.844	288.369	181.143	232.910	225,967	
Ankle yaw	R	133.857	124.980	131.836	127.002	127.881	133.857	
		199.951	205.752	270.967	143.789	199.424	196.611	
Ankle roll	R	158.643	153.633	157.412	154.600	158.906	159.697	
		185.977	204.785	177.012	188.965	202.764	185.977	

Fig 23. Right Kick – Hip Roll

Fig 28. Right Kick – Front View

Fig 29. Right Kick – Side View

Fig 30. Walk Ready

Fig 31. Stand on One Leg

Fig 32. Swinging The Right Leg

Fig 33. Kick The Ball

Fig 34. Swinging The Leg

Fig 35. Back to Walk Ready

Fig 36. Polynomial Graph Side Kick **Table 9.** Pose In Value with Record and Play

Fig 37. Side Kick – Hip Yaw

Fig 40. Side Kick – Knee Pitch

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Fig 45.Walk Ready

Fig 46. Stand on One Leg

Fig 47. Swinging The Leg

Fig 48. Kick The Ball

Fig 49. Swinging Back

Fig 50. Back to Walk Ready

he velocity of motion is measured based on the angle values generated and the accumulated travel time to complete one full motion for each joint. The travel time is measured using a stopwatch.

In **Table 10**, the average time to generate a complete motion for each kick (left kick, right kick, and side kick) using the fourth-degree polynomial trajectory-based method can be observed. The table shows the results obtained from conducting 10 experiments and determined using Equation (4).

$$
R(L) = \frac{53.34}{10} = 5.334 s
$$

$$
R(R) = \frac{60.99}{10} = 6.099 s
$$

$$
R(S) = \frac{38.8}{10} = 3.88 s
$$

Based on 10 experimental trials, the average time to generate a complete motion for each kick was as follows: for the left kick, the average time was 5.334 seconds, for the right kick, the average time was 6.099 seconds, and for the side kick, the average time was 3.88 seconds.

Fig 51. Polynomial Step Time Graph

The time to generate motion using the polynomial trajectory method was compared to the previous method, which was record and play. The speed of motion generation using the polynomial trajectory method is shown in **Table 10.** In the record and play method, the time to generate motion is manually inputted during the creation of the motion. The time to generate motion using the record and play method can be observed in **Table 11.**

Table 11. Step Time Motion Record and Play

Meanwhile, the average time required is calculated is :

$$
R(L) = \frac{54.93}{10} = 5.493 s
$$

$$
R(R) = \frac{5.238}{10} = 5.238 s
$$

Fig 52. Step Time Comparison Graph

The test results indicate that the record and play method requires 5.493 seconds for a left kick, 5.238 seconds for a right kick, and 5.430 seconds for a side kick. These values represent the average time taken to execute each kick using the record and play method.

4. CONCLUSION

After completing this research, it can be concluded that:

- 1. Motion trajectory generation based on fourth degree polynomial method is effective in generating motion for R-SCUAD humanoid robot. The test results show that the trajectories generated using this method exhibit smoother and more consistent motion compared to the record and play method.
- 2. The use of polynomial trajectory-based method provides better control over each joint of the robot. This is evident from the comparison graph that demonstrates significant differences between the motion generated by the trajectory-based method and the record and play method. The polynomial trajectory method is capable of generating trajectories that align with the research objectives.
- 3. The time required by the polynomial-based trajectory method to generate movements for the left and right kicks, based on the collected data from 10 trials, is significantly lower compared to the time taken by the record and play method. However, for the side kick movement, the polynomial-based trajectory method proves to be effective.

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